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Third Semester B.E. Degree Examination, Dec.2018/Jan.2019

Engineering Electromagnetics

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing one full question from each module.

Module-1

- 1 a. State and explain Coulomb's law. (04 Marks)
- b. A charge $Q_A = -20 \mu\text{C}$ is located $A(-6, 4, 7)_m$ and $Q_B = 50 \mu\text{C}$ at $B(5, 8, -2)_m$ in free space. Find the force exerted on Q_A by Q_B ? (05 Marks)
- c. Define electric field intensity and electric flux density. (03 Marks)
- d. Calculate the total charge within the volume $0 \leq \rho \leq 0.1$, $0 \leq \phi \leq \pi$, $2 \leq z \leq 4$, $\rho_v = \rho^2 z^2 \sin 0.6\phi$ (04 Marks)

OR

- 2 a. Obtain an expression for electric field due to infinite line charge. (06 Marks)
- b. A charge of $-0.3 \mu\text{C}$ is located at $A(-25, 30, 15)\text{cm}$ and a second charge of $0.5 \mu\text{C}$ is at $B(-10, 8, 12)\text{cm}$. Find E at the origin. (06 Marks)
- c. A uniform line charge of $2 \mu\text{C/m}$ is located on the z-axis. Find E in rectangular coordinates at $P(1, 2, 3)$ if the charge exists from $-\infty < z < \infty$. (04 Marks)

Module-2

- 3 a. State and prove Gauss law and derive first Maxwell's equations from it. (05 Marks)
- b. Given a $60 \mu\text{C}$ point charge located at the origin. Find the total electric flux passing through the closed surface defined by $\rho = 26 \text{ cm}$ and $z = \pm 26 \text{ cm}$. (04 Marks)
- c. State and prove the Divergence theorem. (05 Marks)
- d. Given the electric flux density $D = 0.3r^2 \hat{a}_r$, nc/m^2 in free space. Find E at the point $P(r = 2, \theta = 25^\circ, \phi = 90^\circ)$. (02 Marks)

OR

- 4 a. Prove that the work done in moving a charge in the electric field is
$$W = -Q \int_{\text{initial}}^{\text{final}} E \cdot dl$$
 (06 Marks)
- b. Calculate the work done in moving a 4C charge from $B(1, 0, 0)$ to $A(0, 2, 0)$ along the path $y = 2 - 2x$, $z = 0$ in the field $E = (5x \hat{a}_x + 5y \hat{a}_y) \text{ V/m}$. (05 Marks)
- c. Show that $\nabla \cdot \mathbf{J} = -\frac{\partial \rho_v}{\partial t}$ with usual notations. (05 Marks)

Module-3

- 5 a. Starting from Gauss law, derive Poisson's and Laplace's equations. (04 Marks)
- b. Calculate ρ_v at point P in free space, if $V = 5\rho^2 \cos 2\phi$ at $P(3, \pi/3, 2)$. (06 Marks)
- c. State uniqueness theorem. (02 Marks)
- d. By using Laplace's equation, derive an expression for the capacitance of a parallel plate capacitor. (04 Marks)

OR

- 6 a. State and explain Biot-Savart's law. (04 Marks)
- b. By using Ampere's law, derive an expression for \vec{H} , magnetic field intensity due to a coaxial cable. (06 Marks)
- c. Evaluate both sides of Stokes theorem for the field, $H = (6ay\hat{a}_x - 3y^2\hat{a}_y)$ A/m and the rectangular path around the region $2 \leq x \leq 5$, $-1 \leq y \leq 1$, $z = 0$. Let the positive direction of ds be a_z . (06 Marks)

Module-4

- 7 a. The field $B = (-2a_x + 3a_y + 4a_z)$ mT is present in free space. Find the vector force exerted on a straight wire carrying a current of 12A in the a_{AB} direction. Given $A(1, 1, 1)$ and $B(2, 1, 1)$. (04 Marks)
- b. Two differential current elements, $I_1\Delta L_1 = 3 \times 10^{-6}$ A-m at $P_1(1, 0, 0)$ and $I_2\Delta L_2 = 3 \times 10^{-6} (-0.5\hat{a}_x + 0.4\hat{a}_y + 0.3\hat{a}_z)$ A-m at $P_2(2, 2, 2)$ are located in free space. Find the vector force exerted on $I_2\Delta L_2$ by $I_1\Delta L_1$. (06 Marks)
- c. Find the magnetization in a magnetic material where
- (i) $\mu = 1.8 \times 10^{-5}$ H/m and $H = 120$ A/m
- (ii) $\mu_r = 22$, there are 8.3×10^{22} atoms/m and each atom has a dipole moment of 4.5×10^{-27} A/m².
- (iii) $B = 300 \mu T \times \chi_m = 15$. (06 Marks)

OR

- 8 a. Derive the Magnetic Boundary Condition? (06 Marks)
- b. Let the permeability is $5 \mu H/m$ in the region 1 where $x < 0$ and $20 \mu H/m$ in the region 2 where $x > 0$, and if $H = (300a_x - 400a_y + 500a_z)$ A/m and if there is a surface current density $K = (150\hat{a}_y - 200\hat{a}_z)$ A/m at $x = 0$.
Find (i) $|H_{t1}|$ (ii) $|H_{N1}|$ (iii) $|H_{t2}|$ (iv) $|H_{N2}|$ (06 Marks)
- c. Derive the expression for the energy density in a magnetic field? (04 Marks)

Module-5

- 9 a. State Faraday's laws of electromagnetic induction. Further derive Maxwell's equation from it. (04 Marks)
- b. Find the amplitude of the displacement current density due to an automobile antenna where the magnetic field intensity of an FM signal is $H_x = 0.15 \cos[3.12(3 \times 10^8 t - y)]$ A/m. (06 Marks)
- c. State Maxwell's equation in both Point form and in Integral form. (06 Marks)

OR

- 10 a. Derive the wave equation in one dimension for an EM wave travelling in free space. (06 Marks)
- b. The electric field amplitude of the uniform plane wave in the a_z direction is 250 V/m. If $E = E_x a_x$ and $\omega = 1.00$ Mrad/s, find (i) the frequency (ii) the wavelength (iii) the period (iv) the amplitude of H. (04 Marks)
- c. State and prove Poynting's theorem. (06 Marks)
